

Topic 4 Review Worksheet

Name Key

1. Determine if each is a solution to the system.

a) $(6, -2); \begin{cases} 3x - 2y = 14 \\ 5x - y = 32 \end{cases}$ NO

$3(6) - 2(-2) \neq 14$
 $18 + 4 \neq 14$

b) $(1, 3); \begin{cases} y \leq x + 2 \\ y > 4x - 1 \end{cases}$ NO

$3 \leq 1 + 2$
 $3 \leq 3 \checkmark$

$3 > 4(1) - 1$
 $3 > 3$ NO

2. Maryann and Carlos are each saving for new scooters. So far, Maryann has \$9 saved, and can earn \$6 per hour babysitting. Carlos has \$3 saved, and can earn \$9 per hour working at his family's restaurant. After how many hours of work will Maryann and Carlos have saved the same amount? What will that amount be?

$y = 9 + 6x$
 $y = 3 + 9x$

$x = \#$ of hrs worked
 $y = \text{total } \$$

$9 + 6x = 3 + 9x$

$6 + 6x = 9x$

$6 = 3x$

$2 = x$

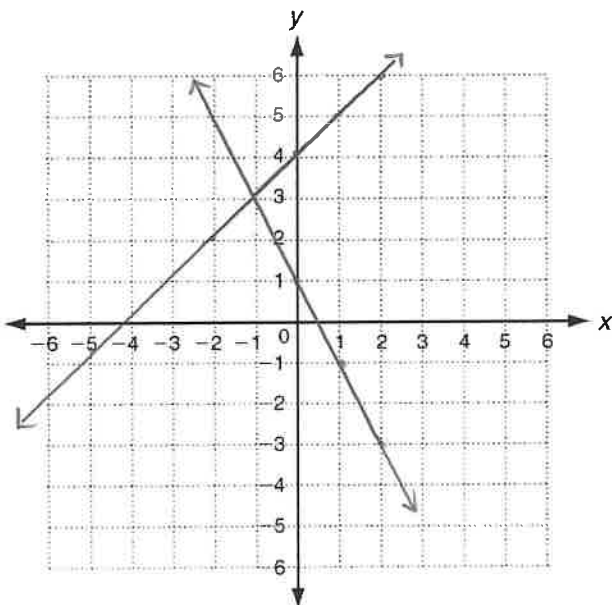
$y = 9 + 6(2)$

$y = 21$

At 2 hrs, they will both have \$21.

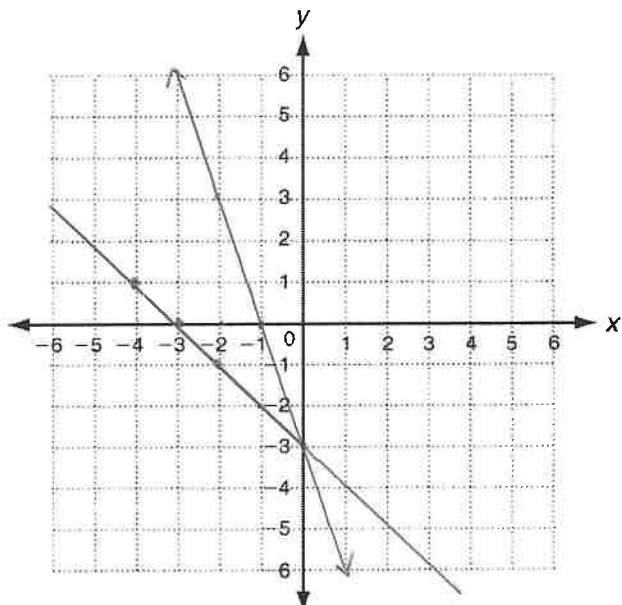
Solve by Graphing.

3. $\begin{cases} y = x + 4 \\ y = -2x + 1 \end{cases}$ Solution: $(-1, 3)$



Solve by Graphing.

4. $\begin{cases} y = -3x - 3 \\ y - 1 = -(x + 4) \end{cases}$ Solution: $(0, -3)$



5. Solve by **Substitution**. $\begin{cases} 4x+y=3.4 \\ x=4y \end{cases}$

$$\begin{aligned} 4(4y) + y &= 3.4 \\ 16y + y &= 3.4 \\ 17y &= 3.4 \\ y &= 0.2 \\ x &= 4(0.2) \\ x &= 0.8 \end{aligned}$$

$$\boxed{(0.8, 0.2)}$$

6. Solve by **substitution**. $\begin{cases} 4x+2y=-2 \\ y=6x-5 \end{cases}$

$$\begin{aligned} 4x + 2(6x-5) &= -2 \\ 4x + 12x - 10 &= -2 \\ 16x - 10 &= -2 \\ 16x &= 8 \\ x &= \frac{1}{2} \\ y &= 6\left(\frac{1}{2}\right) - 5 \\ y &= 3 - 5 = -2 \\ &\boxed{\left(\frac{1}{2}, -2\right)} \end{aligned}$$

7. Solve by **elimination method**.

$$\begin{aligned} 2 \begin{cases} 3x+y=17 \\ 4x+2y=20 \end{cases} &\rightarrow \begin{aligned} -6x-2y &= -34 \\ 4x+2y &= 20 \end{aligned} \\ \hline -2x &= -14 \\ x &= 7 \end{aligned}$$

$$\begin{aligned} 3(7) + y &= 17 \\ 21 + y &= 17 \\ y &= -4 \end{aligned}$$

$$\boxed{(7, -4)}$$

8. Solve by **elimination method**.

$$\begin{aligned} 3 \begin{cases} 4x-y=-5 \\ -2x+3y=10 \end{cases} &\rightarrow \begin{aligned} 12x-3y &= -15 \\ -2x+3y &= 10 \end{aligned} \\ \hline 10x &= -5 \\ x &= -\frac{1}{2} \end{aligned}$$

$$\begin{aligned} 4\left(-\frac{1}{2}\right) - y &= -5 \\ -2 - y &= -5 \\ -y &= -3 \\ y &= 3 \end{aligned}$$

$$\boxed{\left(-\frac{1}{2}, 3\right)}$$

9. Prove that there are infinitely many solutions. What is special about the two equations that makes this happen? Explain.

$$\begin{cases} y=2x-3 \\ y-2x=-3 \end{cases}$$

$$\begin{aligned} 2x-3-2x &= -3 \\ -3 &= -3 \quad \checkmark \end{aligned}$$

Infinite Solutions
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10. Prove that there are no solutions. What is special about the two equations that makes this happen? Explain.

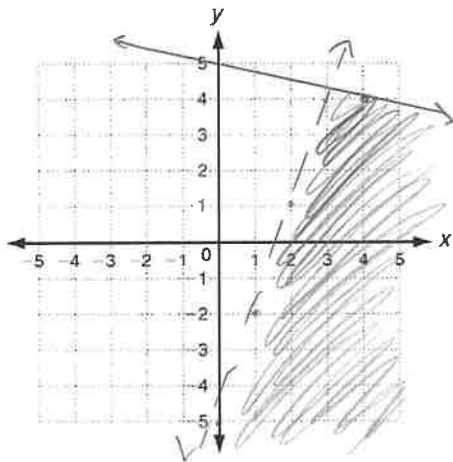
$$\begin{cases} 3x+y=4 \\ -3x=y-7 \end{cases} \rightarrow \begin{aligned} 3x+y &= 4 \\ -3x-y &= -7 \end{aligned}$$

$$\hline 0 \neq -3$$

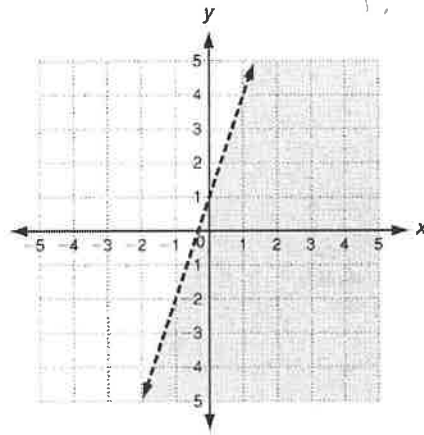
No sol.

11. Graph the system of inequalities. Name two solutions to the system.

$$\begin{aligned} -3x + y < -5 &\rightarrow y < 3x - 5 \\ 4y \leq -x + 20 &y \leq -\frac{1}{4}x + 5 \end{aligned}$$



12. Write the inequality equation for the given graph.



$$y < 3x + 1$$

13. At a pet store, Rhonda paid \$11.50 for 3 dog bowls and 4 bones. Kelly paid \$13 for 2 dog bowls and 8 bones. How much are dog bowls and bones each? Write two equations and solve.

$x = \#$ of dog bowls
 $y = \#$ of bones

$$\begin{aligned} -2(3x + 4y = 11.50) \\ 2x + 8y = 13 \end{aligned}$$

$$\begin{aligned} -6x - 8y = -23 \\ 2x + 8y = 13 \end{aligned}$$

$$-4x = -10$$

$$x = 2.50$$

$$\begin{aligned} \text{Dog Bowls} &= \$2.50 \\ \text{Bones} &= \$1.00 \\ 2(2.50) + 8y &= 13 \\ 5 + 8y &= 13 \\ 8y &= 8 \\ y &= 1 \end{aligned}$$

14. Given the graph below. Write the inequality for each shaded region.

A: $y \geq \frac{1}{2}x + 1$

$$y < -x + 3$$

B: $y \geq \frac{1}{2}x + 1$

$$y > -x + 3$$

C: $y \leq \frac{1}{2}x + 1$

$$y > -x + 3$$

D: $y \leq \frac{1}{2}x + 1$

$$y < -x + 3$$

