

8.5 Systems w/ three variables

Ordered triplet: a solution to a system of equations in three variables.

Ex 1: Is $(-7, 5, 2)$ the solution to the system $2x - 3y = -19 - 5z$

$$2(-7) - 3(5) = -19 - 5(2) \quad -7 + 9(5) - 3(2) = 32 \quad x + 9y - 3z = 32$$

$$-14 - 15 = -19 - 10$$

$$-7 + 45 - 6 = 32$$

$$-4y - 7z = 6x + 8$$

$$-29 = -29 \checkmark$$

$$32 = 32 \checkmark$$

$$-4(5) - 7(2) = 6(-7) + 8$$

Since $(-7, 5, 2)$ is true for all the equations it is the ordered triplet.

$$-20 - 14 = -42 + 8$$

$$-34 = -34 \checkmark$$

Ex 2: Solve the system of equations $x + 3y - z = -10$

$$x = -3y + z - 10 \leftarrow$$

$$-2x + 6y + 3z = 1$$

$$4x - 7y - z = 13$$

$$-2(-3y + z - 10) + 6y + 3z = 1$$

$$4(-3y + z - 10) - 7y - z = 13$$

$$6y - 2z + 20 + 6y + 3z = 1$$

$$-12y + 4z - 40 - 7y - z = 13$$

$$-3(12y + z = -19)$$

$$-19y + 3z = 53$$

$$-36y - 3z = 57$$

$$+ (-19y + 3z = 53)$$

$$\rightarrow -19(-2) + 3z = 53$$

$$38 + 3z = 53$$

$$-55y = 110$$

$$3z = 15$$

$$y = -2$$

$$z = 5$$

$$x + 3(-2) - 5 = -10$$

$$x - 6 - 5 = -10$$

$$x - 11 = -10$$

$$x = 1$$

$$\boxed{(1, -2, 5)}$$

$$\begin{aligned} \textcircled{1} \quad & -r + 2s - 2t = -19 \\ & 5r - s - t = 20 \\ & 4r + 5s + t = 21 \end{aligned}$$

$$r = 2s - 2t + 19$$

$$5(2s - 2t + 19) - s - t = 20$$

$$10s - 10t + 95 - s - t = 20$$

$$9s - 11t + 95 = 20$$

$$*9s - 11t = -75*$$

$$4(2s - 2t + 19) + 5s + t = 21$$

$$8s - 8t + 76 + 5s + t = 21$$

$$13s - 7t + 76 = 21$$

$$*13s - 7t = -55*$$

$$7(9s - 11t = -75) \quad 63s - 77t = -525$$

$$-11(13s - 7t = -55) \quad -143s + 77t = 605$$

$$-80s = 80$$

$$s = -1$$

$$9(-1) - 11t = -75$$

$$-9 - 11t = -75$$

$$-11t = -66$$

$$t = 6$$

$$-r + 2(-1) - 2(6) = -19$$

$$-r - 2 - 12 = -19$$

$$-r - 14 = -19$$

$$-r = -5$$

$$r = 5$$

$$\boxed{(5, -1, 6)}$$

$$\begin{aligned} \textcircled{2} \quad & x - 4y + 4z = 25 \\ & x - 6y + 4z = 27 \\ & -3x - 2y - 4z = -29 \end{aligned}$$

$$(5, -1, 4)$$